A study of the propagation of magnetoacoustic waves in small-scale magnetic fields using solar photospheric and chromospheric Dopplergrams: HMI/SDO and MAST observations

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ABSTRACT

In this work, we present a study of the propagation of low-frequency magneto-acoustic waves into the solar chromosphere within small-scale inclined magnetic fields over a quiet-magnetic network region utilizing near-simultaneous photospheric and chromospheric Dopplergrams obtained from the HMI instrument onboard SDO spacecraft and the Multi-Application Solar Telescope (MAST) operational at the Udaipur Solar Observatory, respectively. Acoustic waves are stochastically excited inside the convection zone of the Sun and intermittently interact with the background magnetic fields resulting into episodic signals. In order to detect these episodic signals, we apply the wavelet transform technique to the photospheric and chromospheric velocity oscillations in magnetic network regions. The wavelet power spectrum over photospheric and chromospheric velocity signals show a one-to-one correspondence between the presence of power in the 2.5-4 mHz band. Further, we notice that power in the 2.5-4 mHz band is not consistently present in the chromospheric wavelet power spectrum despite its presence in the photospheric wavelet power spectrum. This indicates that leakage of photospheric oscillations (2.5-4 mHz band) into the higher atmosphere is not a continuous process. The average phase and coherence spectra estimated from these photospheric and chromospheric velocity oscillations illustrate the propagation of photospheric oscillations (2.5-4 mHz) into the solar chromosphere along the inclined magnetic fields. Additionally, chromospheric power maps estimated from the MAST Dopplergrams also show the presence of high-frequency acoustic halos around relatively high magnetic concentrations, depicting the refraction of high-frequency fast mode waves around $v_A \approx v_s$ layer in the solar atmosphere.

1. Introduction

Acoustic waves are well recognised as an agent of non-thermal energy transfer that couples the lower solar atmospheric layers, primarily through their interactions with and transformations by the highly structured magnetic fields that thread these layers. These waves are generated by turbulent convection within and near the top boundary layers of the convection zone (Lighthill, 1952; Stein, 1967; Goldreich and Kumar, 1990; Bi and Li, 1998) and they resonate to form p-modes in the interior of the Sun. Propagation of these waves into the solar atmosphere is determined by the height dependent characteristic cut-off frequency v_{ac} , which takes the value of ≈ 5.2 mHz for the quiet-Sun photosphere (Bel and Leroy, 1977; Jefferies et al., 2006) as estimated from $\omega_{ac} = 2\pi v_{ac} = c_s/2H_\rho$, where c_s and c_s and c_s are the photospheric sound speed and density scale height, respectively. Height evolution of wave phase in the chromospheric layers at frequencies larger than this cut-off of 5.2 mHz, while evanescent for smaller frequencies, is a well-observed feature in the quiet Sun. However, this condition is altered by the magnetic fields, which affect the propagation of these waves; when plasma ρ is low (ρ <1), acoustic cut-off frequency (c_{ac}) is changed by a factor of $cos \theta$ (Bel and Leroy, 1977; McIntosh and Jefferies, 2006; Cally et al., 2016), where ρ is the angle between the magnetic field and the direction of gravity (which is normal to the solar surface). This fundamental effect of the

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inclined magnetic field has been identified as a key mechanism to tap the energetic low-frequency (*p*-mode) acoustic waves to energise the solar atmospheric layers and was termed as "magnetoacoustic portals" (Jefferies et al., 2006). Sobotka et al. (2013, 2016); Rajaguru et al. (2019); Abbasvand et al. (2020a), and Abbasvand et al. (2020b) have also investigated the propagation of acoustic and magnetoacoustic waves in different magnetic configurations in the lower solar atmosphere. There have also been studies of *p*-mode waves as drivers of impulsive dynamical phenomena that supply mass and energy to the solar atmosphere (De Pontieu et al., 2004, 2005).

In addition to that, we also observe high-frequency power enhancement (above the acoustic cut-off frequency) surrounding the strong magnetic structures such as sunspots, pores, and plages. These excess power enhancements are known as "acoustic halos". This was first observed at the photosphere (Brown et al., 1992) as well as chromosphere (Braun et al., 1992; Toner and Labonte, 1993) in the frequency range v = 5.5-7 mHz, in typically weak to intermediate $(B_{LOS} \approx 50-300 \text{ G})$ photospheric magnetic field regions. The observational studies of halos (Hindman and Brown, 1998; Thomas and Stanchfield, 2000; Jain and Haber, 2002; Finsterle et al., 2004; Moretti et al., 2007; Nagashima et al., 2007) reveal several features, a summary of which has been presented in Khomenko and Collados (2009). Moreover, there is no single theoretical model which can completely explain all the observed features despite having focused efforts (Kuridze et al., 2008; Hanasoge, 2008, 2009; Khomenko and Collados, 2009). The majority of the work emphasizes the interaction of acoustic waves with the background magnetic fields from the photospheric to the chromospheric heights, with regards to power halos observed around the sunspots (Khomenko and Collados (2009) and references therein). However, Krijger et al. (2001), McIntosh and Judge (2001), and McIntosh et al. (2003) have investigated the oscillatons in the network and internetwork regions utililizing observations of lower solar atmosphere from Transition Region and Coronal Explorer (TRACE; Handy et al. (1999)). The physical characteristics of upward propagating acoustic waves are shaped by the topology of nearby magnetic fields. Numerical modelling done by Rosenthal et al. (2002) and Bogdan et al. (2003) show that the propagation of acoustic waves in the solar atmosphere is affected by the magnetic canopy and plasma $\beta \approx 1$ layer where mode conversion, transmission and reflection take place. Khomenko and Collados (2009) utilizing the numerical simulations of magnetoacoustic wave propagation in a magneto-static sunspot model suggest that halos can be caused by the additional energy injected by the high-frequency fast mode waves, which are refracted in the vicinity of the transformation layer (where Alfven speed is equal to the sound speed) in the higher atmosphere due to rapid increase of the Alfven speed. Schunker and Braun (2011) identified some new properties of acoustic halos in active regions. Rajaguru et al. (2013) further explored different properties of high-frequency acoustic halos around active regions including possible signatures of wave refraction utilizing the photospheric velocities, vector magnetograms and lower atmospheric intensity observations.

In this article, we present an analysis of leakage of low-frequency (2.5-4 mHz) acoustic waves into the higher solar atmospheric layers along small-scale inclined magnetic fields of a quiet magnetic network region in the form of magnetoacoustic waves exploiting the high-resolution photospheric velocity observations in Fe I 6173 Å line from Helioseismic and Magnetic Imager (HMI; Schou et al. (2012) instrument onboard the Solar Dynamics Observatory (SDO; Pesnell et al. (2012)) spacecraft and chromospheric velocity estimated from Ca II 8542 Å line scan observations obtained from the Multi-Application Solar Telescope (MAST; Mathew (2009); Venkatakrishnan et al. (2017). It is to be noted that p-mode oscillations are stochastically excited inside the convection zone beneath the solar photosphere and intermittently interact with the background magnetic fields, resulting in episodic signals. Hence, here we employ wavelet analysis to detect these episodic signals propagating from the photospheric to the chromospheric heights using velocity observations. We also investigate the interaction of acoustic waves with the background magnetic fields resulting in the formation of high-frequency acoustic halos in the velocity power maps of a magnetic network region and their relation with the photospheric vector magnetic fields. Our analysis aims to provide insight into the interaction of acoustic waves with small-scale magnetic fields of a quiet network region, depicting different physical phenomena. In the following, Section 2 provides a detailed account of the observational data used in this article, Section 3 discusses the analysis procedure and results obtained from the investigation, and Section 4 provides a further discussion and summary of our results.

2. The Observational data

We employ two-height velocities observed over a magnetic network region in the disc centre to investigate the propagation of *p*-mode waves and appearance of high-frequency power halos and their relation with the background

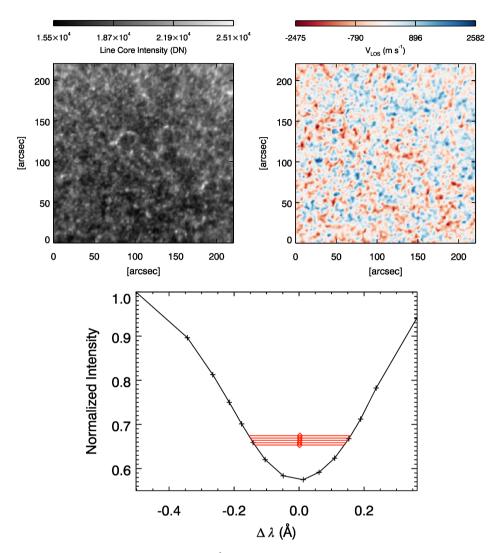


Figure 1: Sample maps of chromospheric Ca II 8542 Å near line-core intensity image (*top left panel*), and chromospheric Dopplergram (*top right panel*) of a quiet magnetic network region observed on May 21, 2020 from the MAST. *Bottom panel* shows a sample profile of Ca II 8542 Å spectral line with five bisector points (red diamond) used to derive the chromospheric line-of-sight Doppler velocity. This profile is constructed from the average intensity over the whole field-of-view (FOV) of the MAST (c.f., *top left panel*). The 15 wavelength locations were scanned in about 15 seconds.

magnetic fields. We use photospheric observations in Fe I 6173 Å spectral line obtained from the HMI instrument onboard the *SDO* spacecraft and chromospheric line-scan observations in Ca II 8542 Å spectral line from the MAST operational at the Udaipur Solar Observatory, Udaipur, India. The following sub-Sections provide brief descriptions of the instruments and data reduction done for the above observations.

2.1. Chromospheric observations in Ca II 8542 Å line from the MAST

The MAST is a 50 cm off-axis Gregorian solar telescope situated at the Island observatory in the middle of Fatehsagar lake at the Udaipur Solar Observatory, Udaipur, India. It is capable of providing observations of the photosphere and chromosphere of the Sun. In order to obtain these observations, an imager optimized with two or more wavelengths is integrated with this telescope. For this purpose, two voltage-tunable lithium niobate Fabry-Perot etalons along with a set of interference blocking filters have been used for developing the Narrow Band Imager (NBI:

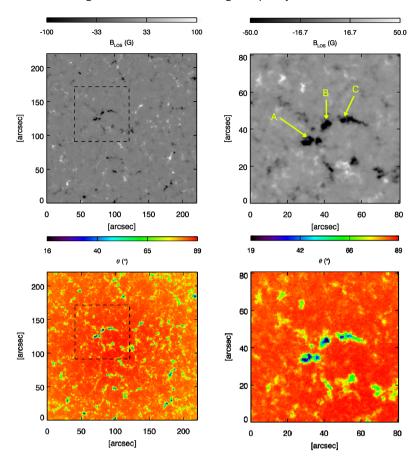


Figure 2: Sample maps of average of photospheric line-of-sight magnetogram over 112 minutes duration (top left panel), blow up region of a strong magnetic network region (top right panel) as denoted by black dashed square box in the top left panel. Line-of-sight (LOS) magnetogram has been saturated at ± 100 G and ± 50 G, respectively, to bring out the small-scale magnetic features. The yellow arrows with labels A', B', and C', show the identified locations for the investigation of leakage of p-mode oscillations. Bottom left panel: Sample map of θ obtained from the HMI vector magnetograms and integrated over the duration of observations. Blow up region illustrating θ of a selected strong magnetic network location (bottom right panel) as denoted by black dashed square box in the left panel.

Raja Bayanna et al. (2014); Mathew et al. (2017)). These two etalons are used in tandem for photospheric observation in Fe I 6173 Å spectral line. However, only one of the etalons is used for the chromospheric observation in Ca II 8542 Å (hereafter Ca II) spectral line. The maximum circular field-of-view (FOV) of the MAST is 6 arcmins, and diffraction-limited resolution is 0.310 arcsec at Fe I 6173 Å wavelength. Utilizing the capabilities of NBI with the MAST, we have observed a magnetic network region in the disk centre in the chromosphere of the Sun. The Ca II line profile has been scanned at 15 different wavelength positions starting from 8541.6 Å to 8542.48 Å within 15 s at a spatial sampling of 0.10786 arcsec per pixel on May 21, 2020, from 04:52:42 - 06:45:20 UT. The core of the line profile is scanned with close sampling intervals, whereas wings are sampled at higher wavelength spacing. Moreover, there is a delay of 19 s between two consecutive line scans. We obtained intensity images at different wavelength positions in a FOV of 220×220 arcsec². The seeing condition was stable during the observation. The top left panel of Figure 1 shows the near-core intensity image of the Ca II line during the starting time of the observations. The bottom panel of Figure 1 shows the Ca II line profile estimated from the average intensity over the full FOV, where plus symbols on the line profile represent the wavelength positions where the line profile has been scanned with the NBI. The centre points of red horizontal lines in the core of the Ca II spectral profile denote the bisector points, which

we have used to estimate the line-of-sight velocity. We have explained the estimation of chromospheric velocity from these observations in Section 3 of this paper.

2.2. Photospheric observations in Fe I 6173 Å line from HMI/SDO

The HMI instrument onboard the SDO spacecraft observes the photosphere of the Sun in Fe I 6173 Å absorption line at six different wavelength positions within ± 172 mÅ window from the centre of Fe I 6173 Å line. It uses two 4096×4096 pixels CCD cameras. One of the cameras, also known as a scalar camera, provides full disc line depth, Dopplergrams, continuum intensity, and line-of-sight magnetic fields at a spatial sampling of 0.504 arcsec per pixel and a temporal cadence of 45 s. The second camera, i.e. vector camera, is dedicated to the measurement of vector magnetic fields of the photosphere of the Sun at the same spatial sampling as scalar camera. It provides full-disk vector magnetograms at a lower cadence (12 minutes) as a standard product, although it can also be obtained at a cadence of 135 s (Hoeksema et al., 2014). To obtain the vector magnetic field observations, Stokes parameters (I, Q, U, V) are observed at six different wavelength positions from the centre of Fe I 6173 Å absorption spectral line profile. Further, to get the information of vector magnetograms of the photosphere from these Stokes parameters, the HMI team utilize Very Fast Inversion of the Stokes algorithm code (VFSIV; Borrero et al. (2011)) to invert the Stokes profiles. The remaining 180 deg. ambiguity in the azimuthal field component is resolved using the minimum-energy method as described by Metcalf (1994), and Leka et al. (2009). Thereafter, these heliocentric spherical coordinates (B_r, B_{θ} , B_{ϕ}) are approximated to (B_z, B_v, B_x) in heliographic cartesian coordinates for ready use in various parameter studies (Gary and Hagyard, 1990). We have photospheric Dopplergrams, line-of-sight magnetograms at 45 s and vector magnetic fields at 12 min cadence. The top left panel of Figure 2 shows the average line-of-sight magnetic field image of the photosphere over the whole observation period as mentioned in Section 2.1 of this paper. We have tracked all these photospheric observables and also removed the differential rotation velocity signals using the Snodgrass formula (Snodgrass, 1984) and the spacecraft velocity from the HMI Dopplergrams.

3. Analysis and Results

In the following, we discuss the analysis procedure of velocities, and magnetic fields over a magnetic network region and results obtained from the investigation.

3.1. Estimation of line-of-sight velocity from Ca II 8542 Å line scan observations from MAST

We resample the Ca II intensity images to match the coarser HMI spatial scale after dark and flat corrections on the line-scan observations obtained from NBI with the MAST. We have used the cross_corr.pro routine available in SolarSoftWare (SSW) to co-align each Ca II intensity image with the previous line scan image. The bisector method (Gray, 2005) has been used to construct chromospheric Doppler velocity. In order to define the reference wavelength, we have used the bisector method on the line profile constructed from the average intensity over full FOV. The bottom panel of Figure 1 shows the Ca II line profile estimated by taking the average over full FOV, with bisector points of five red horizontal lines at different intensity levels in the line core shown by red diamond; the data points marked with plus represent the locations, where the line has been scanned using NBI with the MAST. According to Cauzzi et al. (2008), the wings of the Ca II spectral line that are 0.5 - 0.7 Å away from the line centre map the middle photosphere around h = 200 - 300 km above the $\tau_{500} = 1$ (unity optical depth in the 500 nm continuum) whereas the line core is formed in the height range h = 1300 - 1500 km. Here, we have used bisector in between $\pm 0.14 - 0.18$ Å from the line centre. The contribution in this particular wavelength range comes from a height around $h \approx 900 - 1100$ km (mean height ≈ 1000 km). By taking the average of five bisector points, we obtained a map of $\delta \lambda$, which, after a wavelength shift correction, is then used to estimate the line-of-sight velocity (V_{los}) given by the Doppler shift formula, $V_{los} = (\delta \lambda/\lambda_0)c$, where λ_0 is the rest wavelength, and c is the speed of light. For the wavelength shift corrections, we use a diffuser to take the line-scan observations, which contains only the shift originating from the incident angle (θ) of light. Further, we utilize bisector method to construct map of $\delta \lambda_{shift}$, which is subtracted from $\delta \lambda$ maps. Following this, by combining the time taken for line-scan and delay time, we obtain chromospheric Doppler velocity at a cadence of 34 s. Further, we linearly interpolate over time to match the lower cadence (45 s) photospheric Dopplergrams from the HMI instrument. The interpolated time series (chromospheric Dopplergrams) are now simultaneous to the photospheric Dopplergrams. The top right panel of Figure 1 shows the chromospheric Doppler velocity constructed from MAST observations. For aligning the photospheric and chromospheric observations, we use 20 min averages of line core intensity of Ca II spectral profile and line-of-sight magnetograms and identify similar features for correlation tracking to get sub-pixel

Table 1
Table represents the values of average line-of-sight magnetic fields ($<|B_{LOS}|>$), inclination ($<\theta>$) and cut-off frequency (v_{rr}^B) over selected locations.

Location	<	$< \theta >$ (de-	$v_{ac}^{B} =$
	$ B_{LOS} >$	gree)	$v_{ac}cos\theta$
	(G)		(mHz)
A	42.9	64.2	2.3
В	68.7	58.1	2.7
C	38.5	62.7	2.4

accuracy.

3.2. Photospheric Observables from HMI instrument

We use photospheric Dopplergrams obtained from the HMI instrument, which sample Fe I 6173 Å spectral line. Norton et al. (2006) investigated formation process of Fe I 6173 Å line profile and derive a height range of h = 20300 km above the continuum optical depth ($\tau_c = 1$, which corresponds to z = 0) whereas line continuum is formed around h = 20 km above z = 0. Fleck et al. (2011) used 3d time-dependent radiation hydrodynamic simulation to produce Fe I 6173 Å line profile and calculated Doppler velocity to compare with the observations derived with the HMI instrument. They concluded that V_{HMI} forms at a mean height of 150 km. Other photospheric observables used in this study are B_{IOS} and $B = [B_x, B_y, B_z]$ at a cadence of 45 s and 12 min, respectively. The magnetic fields of the quiet Sun rapidly evolve over a short time duration and decay (Bellot Rubio and Orozco Suárez, 2019). To examine the role of small scale magnetic fields on the leakage of p-mode waves and formation of high-frequency halos, we have taken the average of B_{LOS} over the whole observation duration as shown in the top left panel of Figure 2. The average B_{LOS} map shows only the permanent magnetic features. It has been saturated between ± 100 G to bring out small scale magnetic patches, and a strong network region is selected for final analysis, which is demarcated with a black dashed square box. The top right panel of Figure 2 shows the blow-up region of B_{LOS} . From the vector magnetograms, we have B_x , B_y , and B_z components of the magnetic fields. Similar to Rijs et al. (2016) and Rajaguru et al. (2019), we estimate field inclination $\theta = 90$. $-(180./\pi)|\tan^{-1}(B_z/B_h)|$, where B_z is the radial component of the magnetic fields, and $B_h = \sqrt{B_x^2 + B_y^2}$ is horizontal magnetic fields. Map of θ averged over the whole observation period is shown in the bottom left panel of Figure 2, where $\theta = 0$ degrees corresponds to vertical and $\theta = 90$ degrees represents horizontal magnetic fields. It is to be noted that we have averaged B_{LOS} and θ maps over the whole observation period; this may lead to an averaging out of small scale emerging magnetic fields in between the observation period. Finally, we have selected three different locations ($\{A', \{B', \text{and }\}C'\}$) with magnetic field strength ($\{B_{LOS}\}$) greater than 30 G to study the propagation of p-mode waves from the photosphere into the chromosphere as shown with the yellow arrowheads in the blow-up region of B_{IOS} map (c.f. top right panel of Figure 2), which is our region of interest (ROI). In our analysis, we have considered rasters of 10×10 pixels in the aforementioned identified locations on which the velocity signals are averaged in order to take into account seeing related fluctuations on spatial scales. The values of $<|B_{LOS}|>, <\theta>$ and magnetically modified cut-off frequency $v_{ac}^B=v_{ac}cos\theta$ over locations A', B', and C' are listed in the Table 1.

3.3. Wavelet Analysis of HMI and MAST Velocity Data

In order to detect the presence of episodic wave propagation signals, from the photosphere to the chromosphere through the intermittent interactions between p-modes and the magnetic fields, we have constructed the wavelet power spectrum of the velocity oscillations at the identified locations A', B', and C'.

Wavelet analysis is a powerful technique to investigate non-stationary time series or where we expect localized power variations. Thus, to determine the period of episodic signals present in the identified regions, we apply the wavelet technique (Torrence and Compo, 1998) on the photospheric and chromospheric velocity time series of locations A', B', and C' obtained from HMI and MAST observations. Torrence and Compo (1998) presented a detailed description of the methodology used as the basis for this study. Here, we use the Morlet wavelet, a product of a Gaussian function and a sine wave. In the wavelet power spectrum (WPS), we limit our investigation to a region inside a "cone of influence" corresponding to the periods of less than 25 % of time series length. We have also overplotted the confidence level at 95 % as shown by a solid black line in WPS. For the different locations on the photospheric velocities, we note

the presence of significant power around the 2.5–4 mHz band in WPS, which is associated with the p-mode oscillations (c.f. left panels of Figures 3). The WPS obtained from chromospheric velocities at identified locations also shows the power around 2.5-4 mHz band and above 5.5 mHz (c.f. right panel of Figures 3). Further, the WPS is collapsed over the whole observation time to get the Global Wavelet power spectrum (GWPS). If power is present during the whole length of observation time in WPS, it would also be reflected in the GWPS. The GWPS is similar to the commonly used Fourier power spectrum. In Figures 3 GWPS show the peak around 3 mHz above the confidence level in photospheric and chromospheric locations. Importantly, we note that WPS constructed from the chromospheric velocity time series reveals the presence of significant power around the 3 mHz band at the same time as in the WPS obtained from the photospheric velocity time series (c.f. Figures 3). For instance, significant power is present in the WPS constructed from HMI velocity of location \(A' \) in 0-40 minutes duration in 2.5-4 mHz band (c.f. top left panel of Figure 3), and in the same time interval, we notice significant power in WPS obtained from the chromospheric velocity time series (c.f. top right panel of Figure 3). We have found similar results in other selected locations (c.f. Figure 3). We also notice that despite the presence of significant power in photospheric WPS, we do not see the power in chromospheric WPS. For example prominent power is present in the location B' in 40–100 minute time duration in photospheric WPS (c.f. middle left panel of Figure 3), whereas feeble power is observed in the chromospheric WPS (c.f. middle right panel of Figure 3), pointing that low-frequency acoustic waves intermittently interect with background magnetic fields. We also plot frequency versus height (c.f. Figure 4) of the oscillations observed in the photospheric and chromospheric wavelet power spectrum obtained at two different heights in the solar atmosphere. In the photospheric WPS, we see the presence of dominant 5-min (3.3 mHz) oscillations, however chromospheric WPS indicate the presence of 1.5, 3.3, and 5.0 mHz oscillations. The presence of 3.3 mHz oscillations in the chromosphere is associated with underlying photospheric oscillations, whereas 1.5 and 5.0 mHz oscillations are chromospheric in nature. These findings are consistent with earlier numerical simulations done by Kraśkiewicz et al. (2019), and Kraśkiewicz et al. (2023), where they have derived the cutoff frequency of upward propagating magnetoacoustic waves. Moreover, the estimated acoustic cut-off frequency (v_{ac}^B) (c.f. Table 1) in the locations mentioned above shows that the quiet-Sun photospheric acoustic cut-off frequency (v_{ac}) is adequately reduced in the presence of inclined magnetic fields. Thus, it indicates that the power present around 2.5-4 mHz band in the chromospheric WPS is possibly associated with the leakage of the photospheric p-mode oscillations into the chromosphere.

3.4. Phase and coherence spectra

Wavelet power spectrums of locations A', B', and C' of chromospheric Doppler velocities show one-to-one correspondence in the v=2.5-4 mHz band with the photospheric 2.5-4 mHz band, suggesting that chromospheric power in 2.5-4 mHz band are related to the leakage of photospheric p-mode oscillations. Hence, we estimate the phase and coherence spectra over the region of interest (ROI) (c.f. right panel of Figure 2). We would like to mention here that, spatial maps of phase and coherence do not show clear one-to-one correlations. It might be due to the larger height difference between the photospheric and the chromospheric Dopplergrams, and also due to non-achievement of sub-pixel accuracy in the alignment of the HMI and the MAST observations due to seeing fluctuations. Hence, we have not included these maps in our results. Here, we present the average phase and coherence over the ROI. In order to estimate the phase and coherence between two signals at each pixel, we calculate the cross-spectrum of two evenly sample time series (I_1 and I_2) in the following way:

$$X_{12}(\nu) = I_1(\nu) \times I_2^*(\nu) \tag{1}$$

Where I's are the Fourier transforms, and * denotes the complex conjugate. The phase difference between two-time series is estimated from the phase of complex cross product $(X_{12}(\nu))$

$$\delta\phi(v) = tan^{-1}(Im(\langle X_{12}(v) \rangle)R(\langle X_{12}(v) \rangle))$$
 (2)

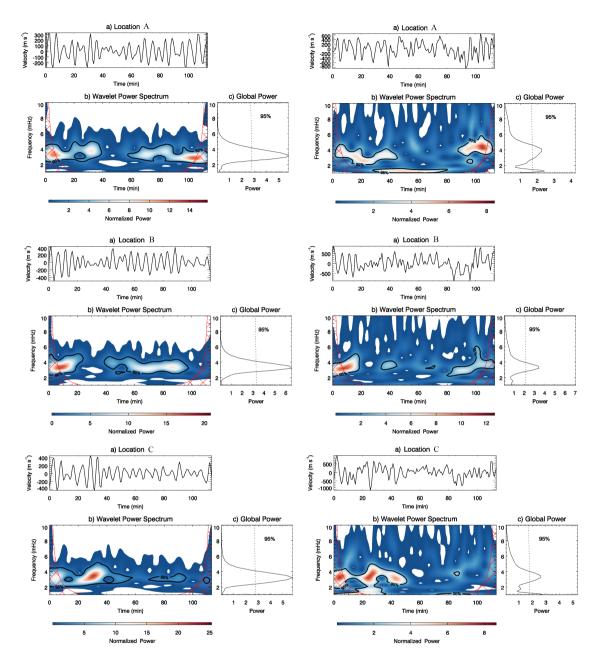


Figure 3: Top left panel: Upper panel (a) shows the temporal evolution of average velocity signals obtained from the photospheric Dopplergrams for the location \(\crit{A}'\). Bottom panel shows the WPS and the GWPS in (b) and (c), respectively, computed from velocity time series. In the WPS, the solid lines demonstrate regions with the 95% confidence level, and the hatched region indicates the cone of influence. The colour scale represents the wavelet power. The dotted line in GWPS shows a confidence level at 95%. Top right panel: Same as top left panel, but from chromospheric velocity for location \(\crit{A}'\) as estimated from MAST observations. Middle and bottom panels are for the locations \(\crit{B}'\) and \(\crit{C}'\), respectively.

We are adopting the convention that positive $\delta\phi(\nu)$ means that signal 1 leads 2, i.e., a wave is propagating from lower height to upper height and vice-versa. Further, the magnitude of $X_{12}(\nu)$ is used to estimate the coherence (C), which ranges between 0 to 1.

$$C(v) = sqrt(|\langle X_{12}(v) \rangle|^2 / \langle |I_1|^2 \rangle \langle |I_2|^2 \rangle)$$
(3)

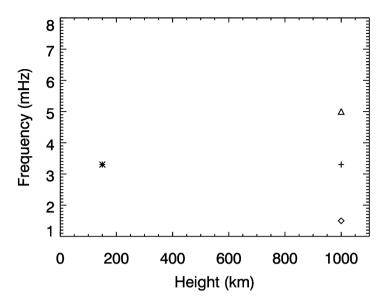


Figure 4: Plot shows the frequency versus height of the oscillations observed in the photospheric and chromospheric wavelet power spectrum. In this plot, the asterisk shows the dominant photospheric frequency observed at 3.3 mHz, whereas the diamond, plus, and triangle represent the chromospheric frequencies observed at 1.5, 3.3, and 5.0 mHz, respectively. The presence of 3.3 mHz oscillations in the chromosphere is associated with the leakage of underlying photospheric oscillations along the inclined background magnetic fields.

Where < . > denotes the average. Coherence is a measure of the linear correlation between two signals, 0 indicates no correlation and 1 means perfect correlation. In our case, we have averaged over segments of length 76 data points, which correspond to 57 minutes at a cadence of 45 seconds. We assume that this is the better way to estimate the $\delta\phi(v)$ and C(v) due to the intermittent nature of the interaction of acoustic waves with the background magnetic fields (Rajaguru et al., 2019).

Figure 5 shows the average phase (black) and coherence (red) spectra between photospheric and chromospheric Doppler velocity observations estimated over the region of interest (ROI) as shown by the black dashed square box on the left panels of Figure 2, and blow up region of the same is depicted in the right panels of Figure 2. In between the photosphere and the chromosphere, atmospheric gravity waves also contribute to the $\delta\phi$. Gravity waves show the negative phase propagation while transporting energy in the upward direction in the lower frequency band in $k-\omega$ diagram (Straus et al., 2008). In our analysis, we also found the negative $\delta\phi$ in the phase estimation from the photospheric and the chromospheric velocities. This is possibly associated with the contribution of gravity waves. However, we found that $\delta\phi$ started increasing around $\nu=3.5$ mHz and continue up to $\nu=6.5$ mHz after which it decreases. The decline of $\delta\phi$ after 6 mHz is possibly associated with steepening of acoustic waves into the shocks. Moreover, the coherence is above 0.5 up to 6 mHz and then slightly decreases. Overall, the estimated average phase and coherence spectra from photospheric and chromospheric velocities indicate the propagation of p-mode waves and are qualitatively in agreement with phase travel time estimated by (Rajaguru et al., 2019) utilizing the photospheric and lower chromospheric intensity observations.

3.5. Photospheric and chromospheric behaviour of high-frequency acoustic halos

The propagation of acoustic waves into the higher solar atmospheric layers in magnetized regions results into different physical phenomena. One of them is the formation of high-frequency acoustic halos. To gain an insight into the interaction of acoustic waves with the background magnetic fields in the quiet magnetic network region (where the magnetic field strength is typically small), we have constructed power maps in different frequency bands, i.e. $\nu = 6, 7, 8, 0$, and 9 mHz from photospheric and chromospheric velocities over a strong magnetic network region as indicated in the top left panel of Figure 2 by the black dashed square box and blow up region of the same is shown here in the top right panel. These maps are integrated over ± 0.5 mHz frequency band around the center as frequency mentioned on

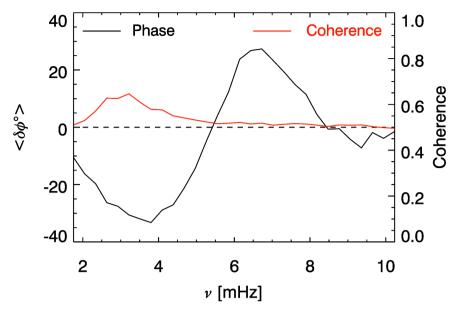


Figure 5: Spatially averaged phase and coherence spectra estimated from photospheric and chromosphere Doppler velocities over region of interest (ROI) as shown in the right panels of Figure 2.

the top of each maps (c.f. Figure 6). Photospheric and chromospheric power maps are shown in the left and right panels of Figure 6, respectively. We do not see high frequency power halos in the photospheric power maps (c.f. left panels of Figure 6) surrounding strong network region. However, chromospheric power maps show high frequency acoustic halos around the magnetic network region at v = 6, 7, 8, and 9 mHz maps as shown in the right panels of Figure 6. In the centre of strong magnetic network concentrations, chromospheric power is suppressed (c.f. right panels of Figure 6). It is to be noted that the magnetic fields of network region spread and diverge at chromospheric height and become significantly inclined in higher atmosphere and changing the height of $\beta = 1$ layer. In our analysis, significant enhancement in chromospheric power is observed in areas surrounding the strong magnetic network region in the form of patches. Further, to better understand the behaviour of high-frequency acoustic halos with respect to photospheric magnetic fields, we have averaged power over a bin of 10 G in $|B_{LOS}|$ and 4-degree bin in θ . Photospheric and chromospheric power as a function of photospheric $|B_{LOS}|$ and θ (integrated over whole observation period) are shown in the top and bottom panels of Figure 7, respectively. It is to be noted that Rajaguru et al. (2013) have estimated power over different ranges of magnetic field strength and inclination from the analysis of different active regions. However, we investigate halos in a quiet magnetic network region, where the magnetic field strengths are much smaller compared to active regions. Photospheric power as a function of $|B_{LOS}|$ shows that more power is present in the 2.5–4.5 mHz band in relatively small magnetic field strengths with more inclined magnetic field regions (c.f. top panels of Figure 7). Interestingly, chromospheric power as a function of photospheric $|B_{LOS}|$ and θ shows that excess power in the high-frequency ($\nu > 5$ mHz) band is present in the small magnetic field strength ($|B_{LOS}| < 60$ G) and more inclined magnetic field regions ($\theta > 60$ degree) (c.f. bottom panel of Figure 7).

4. Discussion and Conclusion

Understanding the physics of interactions between acoustic waves and magnetic fields requires identifying and studying the observational signatures of various associated phenomena in the solar atmosphere, viz. mode conversion, refraction and reflection of waves, formation of high-frequency acoustic halos etc. Most of the work in this field emphasizes the propagation of acoustic waves and their interaction within the highly magnetized regions like sunspots and pores. However, it is not well understood as whether we also expect similar behaviour in a quiet magnetic network region. Multi-height observations covering photospheric and chromospheric layers, especially through intensity imaging observations, are widely used towards the above. Simultaneous velocity observations of both photospheric and

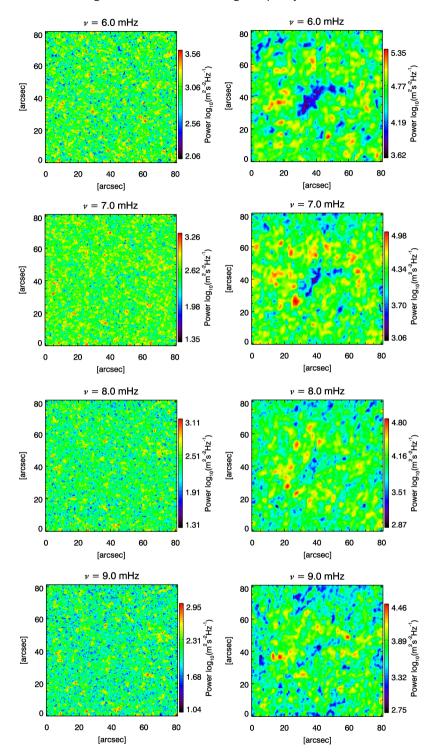


Figure 6: Left panel: Power maps at different frequencies constructed from photospheric velocity obtained from HMI instrument over a small strong magnetic network region as shown in the right panels of Figure 2. Right panel: Same as left panel but from chromospheric velocity estimated from MAST observations.

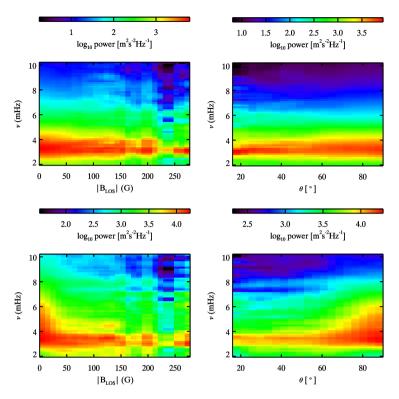


Figure 7: Top panel: Photospheric power are averaged over photospheric magnetic fields, 10 G bins in $|B_{LOS}|$ (left hand side) and 4 degree bins in θ (right hand side), respectively, over a magnetic network region as shown in the right panels of Figure 2. Bottom panel: Same as top panel, but estimated from chromospheric power over photospheric magnetic fields ($|B_{LOS}|$ and θ), respectively.

chromospheric heights are however rare. In this work, in order to address some of the above questions, we have observed a quiet-Sun magnetic network region in the chromospheric Ca II 8542 Å line using the NBI instrument now operational at MAST/USO. Using spectal scans of this region, we have derived chromospheric Doppler velocities. Simultaneous photospheric Doppler velocity and vector magnetic field of this region was also extracted from SDO/HMI data.

We employ wavelet analysis technique to investigate the intermittent interaction of low-frequency (2.5–4.0 mHz) acoustic waves with background magnetic fields in the velocity oscillations at the photospheric and the chromospheric heights using the aforementioned observations. Therefore, we have estimated wavelet power spectra in the selected locations to investigate the propagation of low-frequency acoustic waves from the solar photosphere into the chromosphere as magnetoacoustic waves. These waves are now recognized as a potential candidate to heat the lower solar atmosphere. The investigation of Jefferies et al. (2006) utilizing the velocity observations shows that low-frequency magnetoacoustic waves can propagate into the lower solar chromosphere from the small-scale inclined magnetic field elements. Later on, the detailed investigation done by Rajaguru et al. (2019) provides evidence that a copious amount of energetic low-frequency acoustic waves channel through the small-scale inclined magnetic fields. Usually, acoustic waves of frequency less than photospheric cut-off frequency ($v_{ac} \approx 5.2 \text{ mHz}$) are trapped below the photosphere in the quiet Sun. However, the presence of magnetic fields alters the cut-off frequency, and it is reduced by a factor of $\cos\theta$: $v_{ac}^B = v_{ac} \cos\theta$ (Bel and Leroy, 1977). In our analysis, we have found a significant reduction in the acoustic cut-off frequency, following the above formula, in the presence of inclined magnetic fields. Thus, the presence of low-frequency acoustic waves in the chromospheric wavelet power spectra is clearly associated with the leakage of photospheric oscillations. Moreover, the WPS of both heights show a clear association of chromospheric (5-min) oscillations with the underlying photospheric oscillations as evident from the appearance of low-frequency acoustic waves in chromospheric WPSs approximately at the same time as in the photospheric WPS. The investigation of the average phase over the ROI (80×80 arcsec², c.f. right panel of Figure 2) also shows the turn-on positive phase

around v = 3.5 mHz and continues upto 6.5 mHz, indicating the channelling of photospheric p-mode oscillations into the chromosphere. Additionally, the estimated coherence is above 0.5 up to around 8 mHz, and then it decreases. Nevertheless, the bigger height difference between the two observables also reduces the coherence because these waves travel a long distance, hence losing coherency. Our results are consistent with the previous findings related to the leakage of p-mode oscillations into higher solar atmospheric layers along inclined magnetic fields (De Pontieu et al., 2004, 2005; Jefferies et al., 2006; Vecchio et al., 2007; Rajaguru et al., 2019). However, our results add to the previous findings by illustration of a one-to-one correspondence between oscillatory signals present in the WPS of photospheric and the chromospheric velocity observations of a quiet-Sun magnetic network region. Nevertheless, we also note that leakage of low-frequency acoustic waves along the inclined magnetic fields is not a continuous process, indicating that energy flux estimated from short duration observations could be underestimated or overestimated.

As regards the formation of high frequency acoustic halos surrounding magnetic concentrations, the information gathered from the same is also important to map the thermal and magnetic structure of different heights in the solar atmosphere. The theoretical investigations of Rosenthal et al. (2002), and Bogdan et al. (2003) discussed the effect of magnetic canopy present in the solar atmosphere and plasma $\beta \approx 1$ location. The plasma $\beta \approx 1$ separates two different regions of gas and magnetic pressure dominance. Gary (2001) provided a model of plasma β variation with height in the solar atmosphere over a sunspot and a plage region. Figure 3 of Gary (2001) shows that β is ≈ 1 for plage region at a height of around 1 Mm, while for sunspot it lies below. It is suggested that mode conversion, transmission, and reflection of waves occur at $\beta \approx 1$ (Rosenthal et al., 2002; Bogdan et al., 2003; Khomenko and Collados, 2006, 2009; Khomenko and Cally, 2012; Nutto et al., 2012). The numerical simulation of Khomenko and Collados (2009) proposes that high-frequency fast mode waves which refract in the higher atmosphere around $\beta \approx 1$ due to rapid increase of the Alfven speed can also cause high-frequency acoustic halos around sunspots. Further, they have added that high-frequency halos should form at a distance where the refraction of fast mode acoustic wave occurs above the line formation layer, i.e., where the Alfven speed is equal to sound speed above the photosphere. Else, it would not be possible to detect these halos in observations. We have found high-frequency acoustic halos around a high magnetic concentrations in quiet magnetic network region in the chromospheric Fourier power maps (c.f. right panels of Figure 6). However, halos are not observed in the photospheric power maps. The absence of the acoustic halos in photospheric power maps indicate that formation height of photospheric velocity is far below the mode conversion layer i.e., $\beta \approx 1$, as suggested by Khomenko and Collados (2006) and Rajaguru et al. (2013). Therefore, the presence of halos in the chromospheric power maps is possibly associated with the injection of high frequency fast mode waves, which are refracting from the magnetic canopy and $\beta \approx 1$ layer as proposed by Khomenko and Collados (2009) and Nutto et al. (2012). This fact is also supported by a model of plasma β variation in the solar atmosphere (Gary, 2001) suggesting that $\beta \approx 1$ at a height of ≈ 1000 km over a plage region. For a quiet magnetic network region like ours, we do expect that $\beta \approx 1$ layer might be above 1000 km. The presence of high-frequency acoustic halos in chromospheric power maps is consistent with the explanation provided by Khomenko and Collados (2006, 2009); Kontogiannis et al. (2010); Nutto et al. (2012), and Rajaguru et al. (2013). The chromospheric power maps also show the power deficit in the high magnetic concentrations in the quiet magnetic network region. This could be associated with the energy loss due to the multiple mode transformations in a flux tube (Cally and Bogdan, 1997). The analysis of chromospheric power dependence on photospheric $|B_{LOS}|$ and θ shows that high-frequency power is also significantly present in the small magnetic field strength and in nearly horizontal magnetic field regions. This finding is qualitatively in agreement with the earlier work (Schunker and Braun, 2011), which suggests that the excess power in high-frequency halos is present at the more horizontal and intermediate magnetic field strength region. Our results thus show that small scale magnetic fields also have a significant effect on the propagation of acoustic waves in the solar atmosphere. It is to be noted that we have utilized high resolution photospheric and chromospheric Doppler velocities to investigate the interaction of acoustic waves with the small scale magnetic fields. We intend to follow up with similar analyses using near-simultaneous multi-height velocity and magnetic field observations from MAST and the newer Daniel K Inouye Solar Telescope (DKIST; Rimmele et al. (2020)) along with HMI and AIA instruments on board SDO spacecraft.

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